

METR4202 -- Robotics

Tutorial 4 – Week 4: Robot Dynamics and Control

Reading

Please read/review chapter 8 & 9 of Robotics, Vision and Control.

Review: Forward Kinematics of a two-link planar manipulator

$$x = a_1 \cos \theta_1 + a_2 \cos(\theta_1 + \theta_2)$$

$$y = a_1 \sin \theta_1 + a_2 \sin(\theta_1 + \theta_2)$$

Questions

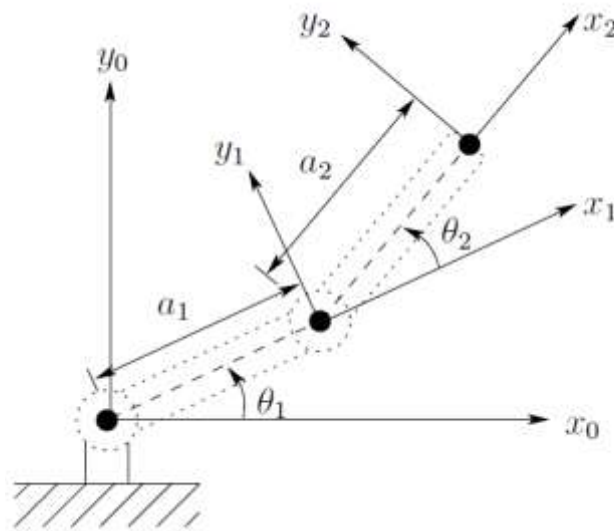


Figure 1: Two-link planar manipulator

1.
 - a.) Using the two-link planar manipulator from tutorial 3, calculate the jacobian needed to relate the joint velocities to the tool-point velocities.
 - b.) Similarly, calculate the inverse jacobian needed to relate the tool-point velocities to the joint velocities.
2.
 - a.) Using the Jacobian found in Q1a, calculate the tool point linear velocity if joint 1 is rotating at 1 rad/s and joint 2 is rotating at 3 rad/s.
 - b.) Calculate the resulting joint torques τ , given a force $F = (30, -20)$ is applied to the end effector tool point.

3.

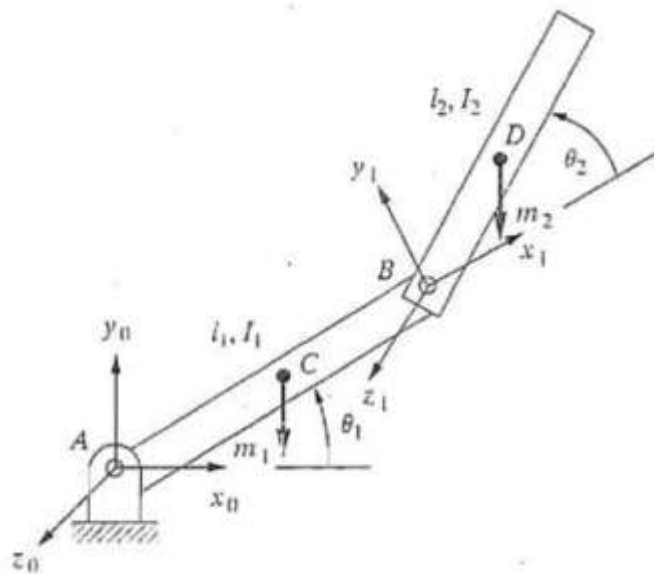


Figure 2: Two-link revolute joint arm.

- a.) With respect to figure 2 above, derive the equations of motion for the two-degree-of-freedom robot arm using the Lagrangian method.

Recall:

Mass Moment of inertia of a slender rod:

Taken about the center of mass:

$$I = \frac{1}{12}ml^2$$

Taken about a fixed axis of rotation:

$$I = \frac{1}{3}ml^2$$

Potential Energy = mgh

Challenge Question:

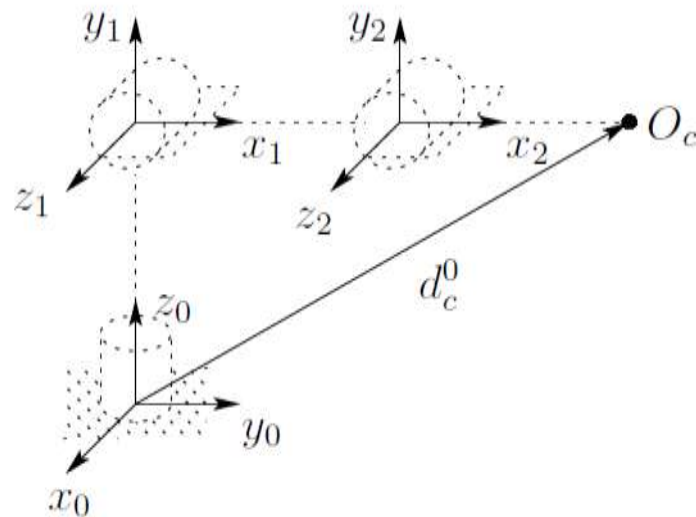


Figure 3: Elbow Manipulator

- List the DH parameters for this arm, clearly indicating which parameters are the joint variables.
- Find the inverse Kinematic equations for the arm to derive the joint values from tool point position.
- Given that the tool point is at $(1.0\text{m}, 0.2\text{m}, 0.5\text{m})^T$, use the inverse kinematic equations to find the joint values.
- Find the manipulator Jacobian, J , that relates the joint velocities to the tool point velocity.